

- Solve the following circuit for the node  $x_1$  and the currents  $y_1$ ,  $y_2$  and  $y_3$ . Use the Fundamental Equation (7) from your textbook to solve first for  $x$  and then for the vector  $y$ . The voltage sources  $\mathbf{b} = (b_1, b_2, b_3)$  are shown in the circuit. The circuit does not have any current sources  $f$ , but ammeters are provided that give you the solution to the currents  $y_1$  and  $y_2$ . You should use these current values only to check your answers, not to obtain the solution. Note the ammeter currents are given in  $\text{mA} = 0.001\text{A}$ . Your solution will be given in  $\text{A}$  (Amperes). You should be able to do

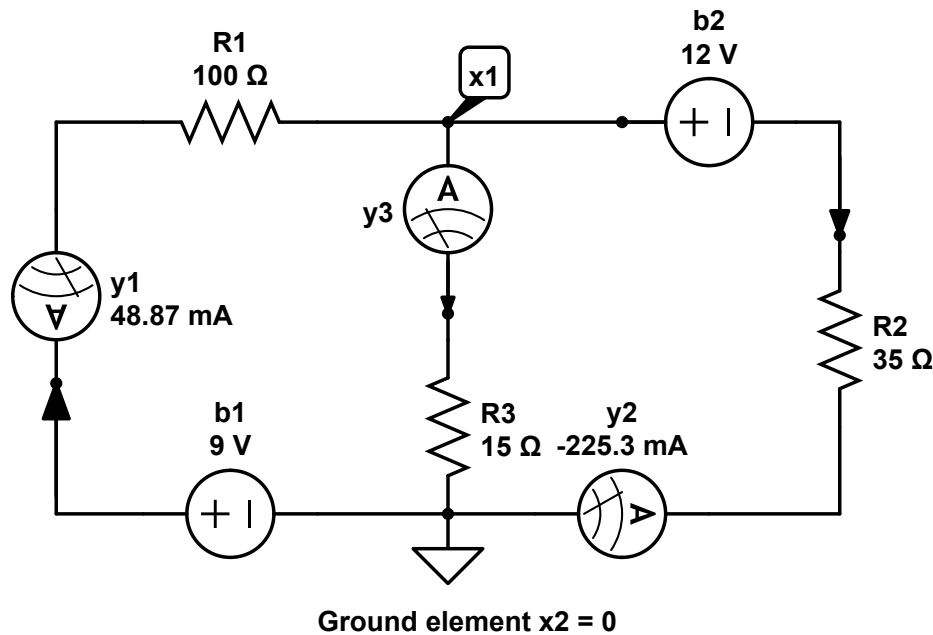


Figure 1: Circuit for problem Problem 1.

the calculations with a calculator, but you may also use Matlab or some other matrix program. In any case, you must show the matrix  $A$  you construct, the equations that you solved, and provide your node and current solutions to four digits of accuracy.

*This circuit was designed in Circuit Lab ([www.circuitlab.com](http://www.circuitlab.com)). Feel free to sign up for a (free) account, replicate and solve this circuit online and check your solution.*

- Problem set §2.5, exercises 1, 2, 6, 8, and 10.

- For each problem, let  $V$  be the space spanned by the given vectors. Find a basis for the orthogonal complement of  $V$ .

- Find a basis for the orthogonal complement of the vector:  $\begin{bmatrix} 2 \\ -1 \\ \frac{1}{2} \end{bmatrix}$ .

(b) Find a normal vector for the plane spanned by the two vectors:  $\begin{bmatrix} 1 \\ 3 \\ 4 \end{bmatrix}$ ,  $\begin{bmatrix} 5 \\ 2 \\ 7 \end{bmatrix}$ .

(c) Find a basis for the plane orthogonal to the plane spanned by the two vectors:

$$\begin{bmatrix} 1 \\ 2 \\ -5 \\ 8 \end{bmatrix}, \begin{bmatrix} -1 \\ -1 \\ 3 \\ -5 \end{bmatrix}.$$

4. Imagine a matrix  $A$  such that the columns of  $A$  add up to the  $\mathbf{0}$  vector, and the rows of  $A$  add up to the  $\mathbf{1}$  vector (vector of all 1's). Show that this is impossible!
5. Problem set §3.1, exercises 5, 26, 27, 32, and 40