

1 First Problem part (a):

The solutions I received seemed dogged by scads of extra variables. I would prefer that the variables in the problem statement be used, while additional needed variables be described and related to the problem statement. Things to watch for:

- (a) $\mathbf{Y} \neq \mathbf{y}$, so it's important to write so that the reader (dirty bifocals and not very swift, as they say) can tell which is meant.
- (b) Ditto for $\mathbf{l} \neq \mathbf{L}$ or $\ell \neq L$.
- (c) Common variables used but not introduced formally: \mathbf{W} , \mathbf{m} , \mathbf{r} (obviated by \mathbf{A}), ∂ , ρ_L .

A dearth of relevant verbiage was endemic.

I have received one acceptable solution for part (a). While this paper did have a couple of extra-ish variables, they were described with brief lines of prose.

But the best feature of this paper's part-(a) solution was that, after the variables were all set up, it stated (in brief *prose*) the basic, fundamental, driving physical principle from which the part-(a) formula derives. Then it proceeded to transform this principle into the formula.

I did receive a further acceptable part-(a) solution. A little short on expository paragraphs, but acceptable.

2 First Problem part (b):

Again, successful solutions depended on deriving the equation from a basic principle. This principle needs to be mentioned explicitly, then made over into the equation.

3 Second Problem part (a):

An algebraic approach is likely best.

The text tells us that the differential equation $\mathbf{y}'' + \omega^2 \mathbf{y} = \mathbf{0}$, derived in the first problem, with

$$\omega = \sqrt{\frac{\rho \ell g}{L \rho}},$$

has solutions of the form

$$\mathbf{y}(t) = C_1 \sin(\omega t) + C_2 \cos(\omega t).$$

We know that the larger the parameter ω becomes, the faster the solution oscillates, that is, the shorter its period is.

And so, from the part-(a) picture, we conclude that cylinder number 1 is less dense than cylinder number 2. If ρ_i denotes the density of cylinder number i , then we have the following string of inequality reasoning:

$$\begin{aligned} \rho_1 &< \rho_2 \\ \frac{1}{\rho_1} &> \frac{1}{\rho_2} \\ \frac{\rho \ell g}{L \rho_1} &> \frac{\rho \ell g}{L \rho_2} \\ \sqrt{\frac{\rho \ell g}{L \rho_1}} &> \sqrt{\frac{\rho \ell g}{L \rho_2}} \\ \omega_1 &> \omega_2 \end{aligned}$$

This last inequality tells us that cylinder number 1 bobs the faster.

4 Second Problem part (b):

This is the same as part (a) except that we start with $L_1 < L_2$ and $\rho_1 = \rho_2$.

5 Third Problem part (a):

From the graph of solution $\mathbf{y}(t)$ on page 115, we can see that the period T is given by $T = 2$. Furthermore, $\mathbf{y}_0 = \mathbf{y}(0) = \mathbf{0}$.

6 Third Problem part (b):

If the solution $\mathbf{y}(t)$ has form

$$\mathbf{y}(t) = C_1 \sin(\omega t) + C_2 \cos(\omega t),$$

then the frequency-period relation $\omega T = 2\pi$ tells us that $\omega = \pi$.

Furthermore, examination of the graph tells us first, that $C_2 = \mathbf{0}$, because $\mathbf{y}(0) = C_2 \cos(0)$. And further, looking at the amplitude tells us that $C_1 = \mathbf{6}$, and so

$$\mathbf{y}(t) = \mathbf{6} \sin(\pi t) \quad \text{and so} \quad \mathbf{y}'(t) = \mathbf{6}\pi \cos(\pi t),$$

so that $\mathbf{y}'_0 = \mathbf{y}'(0) = \mathbf{6}\pi \cos(0) = \mathbf{6}\pi$.

The cylinder dimensions are given us as a red herring...