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/m301.sp06/handouts301/t2\_301\_317/review\_suggestions\_2.tex

- 1 This list is not in final form. Like, stuff may yet be added to it.
- 2 Test #1 is
  - Friday
  - 3/17/06.
- 3 The test will cover the material of Assignments #1 – #21, with emphasis on #14 – #21.
- 4 In the old-tests collection:
  - (a) Test #1 is all fair game.
  - (b) Test #2 parts that are fair game:
    - (i) 1(e)
    - (ii) 2 (where *range* is what we call *column space*)
    - (iii) 3 (although *row space* formally hasn't come up in class, this is fair game)
    - (iv) 4
    - (v) 6 (part (B) is part of 4.1: 33)
  - (c) Test-#3 fair-game parts:
    - (i) 2 just (a) and (b), not (c). Corrected
    - (ii) 3 (¿  $\det(\mathbf{F}) = 39$  ?)
    - (iii) 6(B), 6(D), 6(F)
- 5 Know the basic definitions. Here is a list of the ones I believe to be new since test #1. Approach this in the spirit of Assignment #18: “definition + basic theorem”. For many of these, it's helpful to have a list of entities which are examples of the thing being defined, and examples of things that aren't examples of the thing being defined.
  - (a) definition
  - (b) theorem
  - (c) counterexample
  - (d) matrix inverse

- (e) elementary matrix
- (f) determinant of a matrix
- (g) cofactor
- (h) adjugate
- (i) Cramer's rule
- (j) vector space (10 desiderata)
- (k) linear transformation (as extended to abstract vector spaces)
- (l) subspace of a vector space (3 desiderata)
- (m) subspace *spanned* by a set
- (n) basis for a space or subspace
- (o) null space of a matrix
- (p) column space of a matrix
- (q)
- (r)

**6** Computations you need to be able to do:

- (a) Evaluate the determinant of a big matrix:
  - (i) straight from text's first definition
  - (ii) via cofactor expansion along any row or column
  - (iii) via EROs
- (b) Reduce a matrix to reduced echelon form:
  - (i) for its own sweet sake
  - (ii) to solve  $\mathbf{A}\vec{x} = \vec{b}$  for  $\vec{x}$ , given  $\mathbf{A}$  and  $\vec{b}$
  - (iii) to decide invertibility
  - (iv) to decide span membership
  - (v) to get a null-space basis
  - (vi) to get a column-space basis
  - (vii) to evaluate a determinant

(c)

(d)

**7** Theorems. You should know what these theorems say:

(a) Conditions logically equivalent to invertibility (aka the Big Blue Theorem or the Invertible-Matrix Theorem)